

Hydrodynamic Analysis of a Column Structure of a Petroleum Storage Tank

Inegiyemiema Morrision and Nitonye Samson

Abstract— Column structures are used extensively in the Niger Delta Area of Nigeria to position drilling platforms and petroleum storage facilities in the offshore environment. To avoid failure of the structures it is necessary to carry out hydrodynamics analysis of the columns in order for them to withstand environmental forces of wind, wave and current. The designed column will be subjected to other different forms of load such as the dead weight and light weight besides the environmental loads, but the project focuses only on the environmental loads in which environmental data will be obtained from agencies and applied into Morrision's equation to analyse and obtain the von misses stress, tensile stress and compressive stress. The results obtained are verified by carrying out software analysis using ansys. The accepted result is subjected to API Code to ensure that it fails within an allowable limit.

Index Terms— Current, Dead weight, Enviromental forces, Misses stress, Piles, Wave and Wind

1 INTRODUCTION

THE loading condition of this concrete structure will be divided into two categories, known as life loads and dead loads. The dynamic effect that comes out as a result of this type of loading will also be considered. These will include the dead, live, environmental and dynamic loads. Dead loads are the weights of the storage tank and any permanent equipment and appurtenant structure which do not change with the mode operation. Therefore dead load will include:

- Weight of the storage facility in air, including where appropriate the weight of the concrete column.
- Weight of equipment such as appurtenant structures permanently mounted on the storage facility.

Life loads are the loads imposed on the structure during its use and which may change either during a mode of operation or from one mode of operation to another [5]

1 The weight of consumable supplies and liquids in storage tank.

Environmental loads are loads imposed on the storage tank by natural phenomenon including wind, wave current, earthquake etc. In this particular case, we are going to only consider wind, current and wave. This is because the project will be sited in an intermediate water depth of about twenty five point three meters and is not within an earth

quake prone region.

These are loads imposed on the storage tank due to response to an excitation of a cyclic nature or due to reacting impact to impact. Excitation of the structure may be caused by waves, wind or machinery. Impact may be caused by a barge or a boat berthing against the platform or by drilling operations.

1.1 Loading Conditions

Design environmental load conditions can be referred to as those forces imposed on the storage tank structure by the selected design event: whereas, operating environmental load conditions are those forces imposed on the structure by a lesser event which is not severe enough to restrict normal operations.

1.2 Design Loading Conditions:

The Storage tank will be designed for appropriate loading conditions which will result or produce the most severe effects on the structure. The loading conditions should be a combination of environmental conditions and appropriate dead and live loads in the following manner:

- The first condition will be the operating environmental conditions combined with dead loads and maximum live loads appropriate to normal operations of the storage tank
- Secondly the operating environmental conditions combined with dead loads and minimum live loads appropriate to normal operations of the storage tank.
- Thirdly, the design environmental conditions with dead loads and maximum live loads appropriate for combining with extreme conditions.

• Inegiyemiema Morrision, Department of Marine Engineering, Rivers State University of Science and Technology, Port Harcourt, Rivers State Nigeria. E-mail: ineng22002@yahoo.com
• Nitonye Samson, Department of Marine Engineering, Rivers State University of Science and Technology, Port Harcourt, Rivers State Nigeria. E-mail: nitonyes@yahoo.com

- Fourthly, the design environmental conditions with dead loads and minimum live loads appropriate for combining with extreme conditions.

Hydrostatic forces acting on the structure below the water line including external pressure and buoyancy is my main focus on this project.

The fixed storage facility will be situated in an intermediate water depth; therefore the loads can be represented by their static equivalents. That means the static analysis is adequate enough to describe the true dynamic loads induced by the structure [2].

The steps and method employed in calculation of deterministic static design wave forces on a fixed storage tank. We assume that there is no dynamic response and there is no distortion of the incident wave by the storage facility. The procedure for a given wave directions begins with the specification of the design wave height and associated wave period, storm water depth and current profile. The procedure for the calculation of the wave force follows these steps.

- An apparent wave period is determined which accounts for the Doppler effect of the current on the wave.
- The two-dimensional wave kinematics will be determined from an appropriate wave theory for the specified wave height, storm water depth and apparent period.
- The horizontal components of wave-induced particle velocities and accelerations will be reduced by the wave kinematics factor, which accounts primarily for wave directional spreading.
- The effective local current profile is determined by multiplying the specified current profile by the current blockage factor.
- The effective local current profile is combined vectorially with the wave kinematics to determine locally incident fluid velocities and accelerations for use in Morrison's equation.
- Member dimensions are increased to account for marine growth.
- Drag and inertia force coefficients are determined as functions of wave and current parameters and member shape, roughness (marine growth), size and orientation.

- Wave force coefficients for the conductor array are reduced by the conductor shielding factor.
- Local wave/current forces are calculated for all storage tank members using the Morrison's equation.
- The global force is computed as the vector sum of all the local forces.

1.3 Current

The current load can be described as the vector sum of the tidal, circulation, and storm generated currents. The offshore location varies with the relative magnitude of these compounds and thus their importance for computing loads. Current Profile: Is to determine the variation of current speed and direction with depth.

Current Force only: where current is acting alone (ie no waves). The drag force according to the API specification will be determined by this equation $dU/dt = 0$

Current Associated with Waves: There can be possible superposition of the current and waves. Where this superposition happens it is necessary the current velocity should be added vectorially to the wave particle velocity before the total force is computed [3].

2 Materials and Methods

The appropriate wave theory that was chosen is the Linear/Airy wave theory. This is because the dimensionless wave steepness and the dimensionless relative depth of the parameters on an ATKINS graph fall on the intermediate water depth. We assume that the fluid layer has a uniform mean depth, and that the fluid flow is inviscid, incompressible and irrotational. The simplest and most applied wave theory is the linear wave theory. It is also called small amplitude wave theory. The wave has the form of a sine curve and the free surface profile is written in the following simple form $\eta = a \sin(Kx - \omega t)$.

2.1 Finite Water Depth

The designed fixed offshore storage facility operates in an intermediate water depth. The following equations will be required to calculate the wave loading on the offshore structure [7] [10].

Note: $\omega = 2\pi/T$, $k = 2\pi/\lambda$,

is the wave number, λ is the wave length, T = wave period, a = wave amplitude, g = acceleration due to gravity, t = time, x = direction of wave propagation z = vertical coordinate, d = water depth, total pressure in the fluid = $p_d - \rho g z + p_o$, p_o = atmospheric pressure

Velocity Potentials

$$\phi = \frac{g\zeta_a \cosh k(z+d)}{\omega \cosh kd} \cos(\omega t - kx) \quad (1)$$

Depression Relation $\frac{\omega^2}{g} = k \tanh kd \quad (2)$

Wave Length $\lambda = \frac{gT^2}{2\pi} \tanh \frac{2\pi}{\lambda} d \quad (3)$

Wave elevation $\zeta = \zeta_a \sin(\omega t - kx) \quad (4)$

Dynamic Pressure

$$P_D = \frac{\rho g \zeta_a \cosh k(z+d)}{\cosh kd} \sin(\omega t - kx) \quad (5)$$

Velocity in x – direction

$$u = \omega \zeta_a \frac{\cosh k(z+d)}{\sinh kd} \sin(\omega t - kx) \quad (6)$$

Velocity in z – direction

$$w = \omega \zeta_a \frac{\sinh k(z+d)}{\sinh kd} \cos(\omega t - kx) \quad (7)$$

Acceleration in x-axis

$$a_x = \omega^2 \zeta_a \frac{\cosh k(z+d)}{\sinh kd} \cos(\omega t - kx) \quad (8)$$

Acceleration in z-axis

$$a_z = -\omega^2 \zeta_a \frac{\sinh k(z+d)}{\sinh kd} \sin(\omega t - kx) \quad (9)$$

2.2 Environmental Data

For inplace analysis, the design storm environment shall be 100years directional independent metocean criteria. The operating environment shall be 1 year directional independent metocean criteria. Tables 1, 2 and 3 below summaries the design criteria [1].

Table1: Environmental Data

			Return periods (yrs)	
			1	100
Max. wave height in the sea state H_s	H_{max}	m	4.8	7.1
Expected associated or spectral peak wave period	T_p	sec	15.3	15.7
1 hour average mean wind speed	U(1hr)	m/sec	12.0	16.3
1 minute average mean wind speed	U (1min)	m/sec	19.6	32.3
Highest 3 seconds gust in the hour	U (3sec)	m/sec	21.5	35.5
Surge		m	0.25	0.5
Surface current		m/sec	1.04	1.44
Current at mid-depth		m/sec	0.87	1.21
Current at 1m above sea level		m/sec	0.50	0.69

Table 2: Hydrodynamic Coefficient

	Inplace Analysis	
	Smooth Surface	Rough Surface
C_d	0.65	1.05
C_w	1.6	1.20

Table 3: Steel Properties

Young's modulus E	205000 MPa
Shear modulus G	80000 MPa
Density	7850
Poisson's ratio	0.3
Coefficient of thermal expansion	$12 \times 10^{-6} / ^\circ C$

2.3 Column Data and Material Properties:

The structure is analysed based on the given column parameters from the table below.

Table 4: Column Geometric characteristics

Height	30m
Length spacing	20m
Width spacing	20m
Submerge Height (d)	25.3m
Diameter (D)	2m
Thickness (t)	0.0m

2.4 Material Properties

All materials specified in this report are of structural steel pipe of Group II Class C ASTM Grade 50 A618 (Young's Modulus 210MPa, Poisons' Ratio of 0.3, Min. Yield Strength of 345MPa and Min. Tensile Strength of 485MPa) [6][8].

2.5 Derived Parameter

The following parameters were derived from the linear wave theory for a finite water depth and are used as input in evaluating the fluid kinematics as well as input for the fluid loading on the structure in the ansys software.

Table 5: Derived parameters to be used

Parameter	Formula	Values	Unit
Wave Amplitude (ζ_a)	H/2	3	m
Wave Frequency (ω)	$\frac{2\pi}{T}$	0.838	Rad/secs
Wave number (K)	$\omega^2/g \tanh(kd)$	0.0748	m^{-1}

N.B this is obtained from iteration process. See table

2.6 Fluid Particle Kinematics: Velocity and Acceleration of Wave particles

- The fluid particle velocity and acceleration were determined using the linear wave theory for a finite water depth shown in table 3. In this report the wave is assumed to approach the structure at an angle assumed to be zero, therefore wave direction

is considered uniform with the direction of the current.

- The calculated wave velocity along the x-axis is then combined with the current's velocity to give the total velocity, U_T .
- The approach assumed there is no interaction between members in close proximity and problem is set up within the frame work of Global axis system.

Transformation

The following transformation matrices were used;

- Vertical members

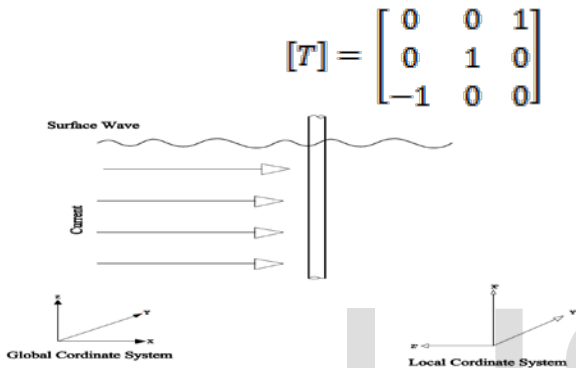


Fig 1: Current direction [4].

2.7 Fluid loading; Morison's equation

The hydrodynamic load acting on the structure was estimated according to the Morison's equation. The Application of this equation is based on the assumption that the ratio of member diameter to wave length (D/λ) is less than 0.05. The equation is as given below;

$$f_L = f_D + f_i \tag{10}$$

Where

f_L = force per unit length (N/m)

f_D = drag force term (N/m)

f_i = inertia force (N/m)

The drag and inertia force are calculated using

$$f_D = \frac{1}{2} \rho C_D D W_n |W_n| \tag{11}$$

$$\text{and } f_i = \rho \frac{\pi D^2}{4} C_m \dot{W}_n \tag{12}$$

Therefore the component of force on a member in the local axis system is calculated using

$$\begin{Bmatrix} f'_{y'} \\ f'_{z'} \end{Bmatrix} = \frac{1}{2} \rho C_D D |W_n| \begin{Bmatrix} v'_{w'} \\ w'_{w'} \end{Bmatrix} + \rho \frac{\pi D^2}{4} C_m \begin{Bmatrix} \dot{v}'_{w'} \\ \dot{w}'_{w'} \end{Bmatrix} \tag{13}$$

Where C_D = Drag coefficient=1.05

C_m = Inertia Coefficient=1.2

With each of this forces evaluated at 3m interval spanning

through the length of the members/element. All force calculation was performed in the Micro soft spread sheet. See Appendix A for loads generated [5].

2.8 A Hand Calculation of Morrison's Equation

A sample hand calculation of Morrison's equation is done below for water depth -3 for column number one. This is done to show case the calculation procedure used and to verify the results obtained from the use of the excel spread sheet [2].

$$\frac{\omega^2}{g} = k \tanh kd$$

$$u = \omega \zeta_a \frac{\cosh k(z+d)}{\sinh kd} \sin(\omega t - kx)$$

After substitution

$$u = -1.55 \text{ m/s}$$

$$u_{total} = u_{wave} + u_{current}$$

$$u_{total} = -1.5585 + 16.3 = 14.7415 \text{ m/s}$$

$$a_x = \omega^2 \zeta_a \frac{\cosh k(z+d)}{\sinh kd} \cos(\omega t - kx)$$

After substitution

$$a_x = 1.213 \text{ m/s}^2$$

To find the in-line force at column depth -3m we apply the Morrison's equation

$$\begin{Bmatrix} f'_{y'} \\ f'_{z'} \end{Bmatrix} = \frac{1}{2} \rho C_D D |W_n| \begin{Bmatrix} v'_{w'} \\ w'_{w'} \end{Bmatrix} + \rho \frac{\pi D^2}{4} C_m \begin{Bmatrix} \dot{v}'_{w'} \\ \dot{w}'_{w'} \end{Bmatrix}$$

$$\begin{Bmatrix} f'_{y'} \\ f'_{z'} \end{Bmatrix} =$$

$$\frac{1}{2} \times 1.05 \times 1025 \times 2 \times 14.74 \begin{Bmatrix} 0 \\ 14.74 \end{Bmatrix} + 1.2 \times 1025 \frac{3.14 \times 2^2}{4} \begin{Bmatrix} 0 \\ 1.213 \end{Bmatrix}$$

$$\begin{Bmatrix} 0 \\ 238519.05 \end{Bmatrix} = \begin{Bmatrix} 0 \\ 233834.25 \end{Bmatrix} + \begin{Bmatrix} 0 \\ 4684.8 \end{Bmatrix} \text{ (N/m)}$$

3 Results and Discussion

3.1 The Use of Excel Spread Sheet to Generate the Forces

The forces due to the incident wave and the prevailing current at different depths on the four columns are determined using an excel spread sheet.

All the results obtained from the spread sheet are used in a CFD method to determine the diameter of the column that will be large enough to withstand the stress and forces due to the incident wave and the current. A preliminary column diameter of two meter was first used.

Table 6: Hydrodynamic formulae to be imputed into the excel program

Iteration No	$\omega=2\pi/T$	ω^2	K_i	k_{i+1}	Error= $K_{i+1}-K_i$
1	0.8378	0.7018	0.7018	0.0715	-0.630295
2			0.0715	0.0755	0.003937
3			0.0755	0.0748	-0.000727
4			0.0748	0.0749	0.000123
5			0.0749	0.0749	-0.000021
6			0.0749	0.0749	0.000004
7			0.0749	0.0749	-0.000001
8			0.0749	0.0749	0.000000
9			0.0749	0.0749	0.000000
10			0.0749	0.0749	0.000000
11			0.0749	0.0749	0.000000
12			0.0749	0.0749	0.000000

Table 7: Observed Parameter

Parameter	Values	Units
Wave height, H	6	m,sec
Wave Period, T	7.5	Sec
Design Current, C	16.3	m/s
Wave angle, α	0	degree
Wind velocity	0	m/s
Wave elevation	3	m
Water depth	25.3	m
Time	5.625	Sec
Acceleration due gravity	9.81	m/s ²

CD	1.05
CM	1.2
Density of Water	1025 kg/m ³
Diameter of Pipe	2 m
Thickness	1 m

Table 8 The use of MATLAB to obtain the Constant K_1

Formulae	
Velocity potential	$\phi=g\zeta_0 \cosh k(z+d)\cos(\omega t-kx_c)/\omega \cosh kd$
Dispersion relation	$\omega^2/g=k \tanh kd$
Wave elevation	$\zeta=\zeta_0 \sin(\omega t-kx_c)$
Dynamics pressure	$PD=\rho g \zeta_0 \cosh k(z+d)\sin(\omega t-kx_c)/\omega \cosh kd$
Velocity in x-axis, U	$U=\omega \zeta_0 \cosh k(z+d)\sin(\omega t-kx_c)/\sinh kd$
Velocity in z-axis, W	$W=\omega \zeta_0 \sinh k(z+d)\cos(\omega t-kx_c)/\sinh kd$
acceleration, a_x	$a_x=\omega^2 \zeta_0 \cosh k(z+d)\cos(\omega t-kx_c)/\sinh kd$
acceleration, a_z	$a_z=-\omega^2 \zeta_0 \sinh k(z+d)\sin(\omega t-kx_c)/\sinh kd$
Angular velocity, ω	$\omega=2\pi/T$
Wave elevation, ζ	$H/2$
Time, t	$3T/4$

Table 9: Excel program to generate the environmental forces acting on pillar 1

VERTICAL MEMBER1														
Xi(m)	Yi(m)	Zi(m)	xc=xicosα	Coshk(z+d)	Sinhk(z+d)	Sinhkd	Cos(ωt-kxc)	Sin(ωt-kxc)	U	W	a _x	a _z	U _c =U+C	
-10	-10	0	-10.0000	3.3979	3.2474	3.2474	0.6806	-0.7327	-1.9267	1.7105	1.4994	1.5426	14.3733	
-10	-10	-3	-10.0000	2.7485	2.5602	3.2474	0.6806	-0.7327	-1.5585	1.3485	1.2129	1.2161	14.7415	
-10	-10	-6	-10.0000	2.2383	2.0025	3.2474	0.6806	-0.7327	-1.2692	1.0548	0.9877	0.9513	15.0308	
-10	-10	-9	-10.0000	1.8415	1.5463	3.2474	0.6806	-0.7327	-1.0442	0.8145	0.8126	0.7345	15.2558	
-10	-10	-12	-10.0000	1.5379	1.1684	3.2474	0.6806	-0.7327	-0.8720	0.6155	0.6787	0.5550	15.4280	
-10	-10	-15	-10.0000	1.3123	0.8497	3.2474	0.6806	-0.7327	-0.7441	0.4476	0.5791	0.4036	15.5559	
-10	-10	-18	-10.0000	1.1531	0.5741	3.2474	0.6806	-0.7327	-0.6538	0.3024	0.5088	0.2727	15.6462	
-10	-10	-21	-10.0000	1.0523	0.3275	3.2474	0.6806	-0.7327	-0.5966	0.1725	0.4643	0.1556	15.7034	
-10	-10	-24	-10.0000	1.0047	0.0975	3.2474	0.6806	-0.7327	-0.5697	0.0513	0.4434	0.0463	15.7303	
-10	-10	-25.3	-10.0000	1.0000	0.0000	3.2474	0.6806	-0.7327	-0.5670	0.0000	0.4413	0.0000	15.7330	
Zi(m)	u _g =U _c cosα	vg=ucsina	w _g	ū _g =axcosa	v _g =axsina	w _g	U _L	VL	W _L	ū _L	v _L	w _L		
0	14.3733	0.0000	1.5426	1.4994	0.0000	1.5426	1.5426	0.0000	-14.3733	1.5426	0.0000	-1.4994		
-3	14.7415	0.0000	1.2161	1.2129	0.0000	1.2161	1.2161	0.0000	-14.7415	1.2161	0.0000	-1.2129		
-6	15.0308	0.0000	0.9513	0.9877	0.0000	0.9513	0.9513	0.0000	-15.0308	0.9513	0.0000	-0.9877		
-9	15.2558	0.0000	0.7345	0.8126	0.0000	0.7345	0.7345	0.0000	-15.2558	0.7345	0.0000	-0.8126		
-12	15.4280	0.0000	0.5550	0.6787	0.0000	0.5550	0.5550	0.0000	-15.4280	0.5550	0.0000	-0.6787		
-15	15.5559	0.0000	0.4036	0.5791	0.0000	0.4036	0.4036	0.0000	-15.5559	0.4036	0.0000	-0.5791		
-18	15.6462	0.0000	0.2727	0.5088	0.0000	0.2727	0.2727	0.0000	-15.6462	0.2727	0.0000	-0.5088		
-21	15.7034	0.0000	0.1556	0.4643	0.0000	0.1556	0.1556	0.0000	-15.7034	0.1556	0.0000	-0.4643		
-24	15.7303	0.0000	0.0463	0.4434	0.0000	0.0463	0.0463	0.0000	-15.7303	0.0463	0.0000	-0.4434		
-25.3	15.7330	0.0000	0.0000	0.4413	0.0000	0.0000	0.0000	0.0000	-15.7330	0.0000	0.0000	-0.4413		
angle between the local and global axes			Transformation matrix						Transpose Matrix					
90	90	0	0	0	1	0	0	-1						
90	0	90	0	1	0	0	1	0						
180	90	90	-1	0	0	1	0	0						
	wn=(VL ² +wL ²) ^{1/2}	%CDpDWi	%CMpπD	Fdy	Fdz	Fiy	Fiz	Fx'	Fy'	Fz'	Fx	Fy	Fz	
0	14.37	15469.28	3864.16	0.00	-222344.8	0.00	-5794.00	0.00	0.00	-228139	228139	0.00	0.00	
-3	14.74	15865.58	3864.16	0.00	-233882.9	0.00	-4686.68	0.00	0.00	-238570	238570	0.00	0.00	
-6	15.03	16176.92	3864.16	0.00	-243152.4	0.00	-3816.72	0.00	0.00	-246969	246969	0.00	0.00	
-9	15.26	16419.09	3864.16	0.00	-250486.8	0.00	-3140.07	0.00	0.00	-253627	253627	0.00	0.00	
-12	15.43	16604.34	3864.16	0.00	-256171.0	0.00	-2622.45	0.00	0.00	-258793	258793	0.00	0.00	
-15	15.56	16742.05	3864.16	0.00	-260438.0	0.00	-2237.64	0.00	0.00	-262676	262676	0.00	0.00	
-18	15.65	16839.21	3864.16	0.00	-263469.5	0.00	-1966.17	0.00	0.00	-265436	265436	0.00	0.00	
-21	15.70	16900.73	3864.16	0.00	-265398.1	0.00	-1794.27	0.00	0.00	-267192	267192	0.00	0.00	
-24	15.73	16929.73	3864.16	0.00	-266309.6	0.00	-1713.25	0.00	0.00	-268023	268023	0.00	0.00	
-25.3	15.73	16932.62	3864.16	0.00	-266400.6	0.00	-1705.16	0.00	0.00	-268106	268106	0.00	0.00	
											2557530	0.00	0.00	

Table 10: Excel program to generate the environmental forces acting on pillar 2

VERTICAL MEMEBER2													
Xi(m)	Yi(m)	Zi(m)	xc=xicosα	Coshk(z+d)	Sinhk(z+d)	Sinhkd	Cos(ωt-kxc)	Sin(ωt-kxc)	U	W	a _x	a _z	U _c =U+C
10	-10	0	10.0000	3.3979	3.2474	3.2474	-0.6806	-0.7327	-1.9267	-1.7105	-1.4994	1.5426	14.3733
10	-10	-3	10.0000	2.7485	2.5602	3.2474	-0.6806	-0.7327	-1.5585	-1.3485	-1.2129	1.2161	14.7415
10	-10	-6	10.0000	2.2383	2.0025	3.2474	-0.6806	-0.7327	-1.2692	-1.0548	-0.9877	0.9513	15.0308
10	-10	-9	10.0000	1.8415	1.5463	3.2474	-0.6806	-0.7327	-1.0442	-0.8145	-0.8126	0.7345	15.2558
10	-10	-12	10.0000	1.5379	1.1684	3.2474	-0.6806	-0.7327	-0.8720	-0.6155	-0.6787	0.5550	15.4280
10	-10	-15	10.0000	1.3123	0.8497	3.2474	-0.6806	-0.7327	-0.7441	-0.4476	-0.5791	0.4036	15.5559
10	-10	-18	10.0000	1.1531	0.5741	3.2474	-0.6806	-0.7327	-0.6538	-0.3024	-0.5088	0.2727	15.6462
10	-10	-21	10.0000	1.0523	0.3275	3.2474	-0.6806	-0.7327	-0.5966	-0.1725	-0.4643	0.1556	15.7034
10	-10	-24	10.0000	1.0047	0.0975	3.2474	-0.6806	-0.7327	-0.5697	-0.0513	-0.4434	0.0463	15.7303
10	-10	-25.3	10.0000	1.0000	0.0000	3.2474	-0.6806	-0.7327	-0.5670	0.0000	-0.4413	0.0000	15.7330
Zi(m)	u _c =U _c cosα	vg=ucsinα	w _g	ūg=αxcosα	v̄g=αxsinα	ḡg	U _L	VL	W _L	ūL	v̄L	w̄L	
0	14.3733	0.0000	1.5426	-1.4994	0.0000	1.5426	1.5426	0.0000	-14.3733	1.5426	0.0000	1.4994	
-3	14.7415	0.0000	1.2161	-1.2129	0.0000	1.2161	1.2161	0.0000	-14.7415	1.2161	0.0000	1.2129	
-6	15.0308	0.0000	0.9513	-0.9877	0.0000	0.9513	0.9513	0.0000	-15.0308	0.9513	0.0000	0.9877	
-9	15.2558	0.0000	0.7345	-0.8126	0.0000	0.7345	0.7345	0.0000	-15.2558	0.7345	0.0000	0.8126	
-12	15.4280	0.0000	0.5550	-0.6787	0.0000	0.5550	0.5550	0.0000	-15.4280	0.5550	0.0000	0.6787	
-15	15.5559	0.0000	0.4036	-0.5791	0.0000	0.4036	0.4036	0.0000	-15.5559	0.4036	0.0000	0.5791	
-18	15.6462	0.0000	0.2727	-0.5088	0.0000	0.2727	0.2727	0.0000	-15.6462	0.2727	0.0000	0.5088	
-21	15.7034	0.0000	0.1556	-0.4643	0.0000	0.1556	0.1556	0.0000	-15.7034	0.1556	0.0000	0.4643	
-24	15.7303	0.0000	0.0463	-0.4434	0.0000	0.0463	0.0463	0.0000	-15.7303	0.0463	0.0000	0.4434	
-25.3	15.7330	0.0000	0.0000	-0.4413	0.0000	0.0000	0.0000	0.0000	-15.7330	0.0000	0.0000	0.4413	
angle between the local and global axes			Transformation matrix			Transpose Matrix							
90	90	0	0	0	1	0	0	-1					
90	0	90	0	1	0	0	1	0					
180	90	90	-1	0	0	1	0	0					
wn=(VL ² +wL ²) ^{1/2}	%CDpDW	%CMpnd	Fdy	Fdz	Fiy	Fiz	Fx'	Fy'	Fz'	Fx	Fy	Fz	
0	14.37	15469.28	3864.16	0.00	-222344.8	0.00	5794.00	0.00	0.00	-216550.8	216551	0.00	0.00
-3	14.74	15865.58	3864.16	0.00	-233882.9	0.00	4686.68	0.00	0.00	-229196.2	229196	0.00	0.00
-6	15.03	16176.92	3864.16	0.00	-243152.4	0.00	3816.72	0.00	0.00	-239335.7	239336	0.00	0.00
-9	15.26	16419.09	3864.16	0.00	-250486.8	0.00	3140.07	0.00	0.00	-247346.7	247347	0.00	0.00
-12	15.43	16604.34	3864.16	0.00	-256171.0	0.00	2622.45	0.00	0.00	-253548.5	253549	0.00	0.00
-15	15.56	16742.05	3864.16	0.00	-260438.0	0.00	2237.64	0.00	0.00	-258200.3	258200	0.00	0.00
-18	15.65	16839.21	3864.16	0.00	-263469.5	0.00	1966.17	0.00	0.00	-261503.3	261503	0.00	0.00
-21	15.70	16900.73	3864.16	0.00	-265398.1	0.00	1794.27	0.00	0.00	-263603.8	263604	0.00	0.00
-24	15.73	16929.73	3864.16	0.00	-266309.6	0.00	1713.25	0.00	0.00	-264596.3	264596	0.00	0.00
-25.3	15.73	16932.62	3864.16	0.00	-266400.6	0.00	1705.16	0.00	0.00	-264695.4	264695	0.00	0.00
SUMMATION OF FORCES										2498577	0.00	0.00	

Table 11: Excel program to generate the environmental forces acting on pillar 3

VERTICAL MEMEBER3													
Xi(m)	Yi(m)	Zi(m)	xc=xcosa	Coshk(z+d)	Sinhk(z+d)	Sinhkd	cos(ωt-kxc)	Sin(ωt-kxc)	U	W	a _x	a _z	U _c =U+C
10	10	0	10.0000	3.3979	3.2474	3.2474	-0.6806	-0.7327	-1.9267	-1.7105	-1.4994	1.5426	14.3733
10	10	-3	10.0000	2.7485	2.5602	3.2474	-0.6806	-0.7327	-1.5585	-1.3485	-1.2129	1.2161	14.7415
10	10	-6	10.0000	2.2383	2.0025	3.2474	-0.6806	-0.7327	-1.2692	-1.0548	-0.9877	0.9513	15.0308
10	10	-9	10.0000	1.8415	1.5463	3.2474	-0.6806	-0.7327	-1.0442	-0.8145	-0.8126	0.7345	15.2558
10	10	-12	10.0000	1.5379	1.1684	3.2474	-0.6806	-0.7327	-0.8720	-0.6155	-0.6787	0.5550	15.4280
10	10	-15	10.0000	1.3123	0.8497	3.2474	-0.6806	-0.7327	-0.7441	-0.4476	-0.5791	0.4036	15.5559
10	10	-18	10.0000	1.1531	0.5741	3.2474	-0.6806	-0.7327	-0.6538	-0.3024	-0.5088	0.2727	15.6462
10	10	-21	10.0000	1.0523	0.3275	3.2474	-0.6806	-0.7327	-0.5966	-0.1725	-0.4643	0.1556	15.7034
10	10	-24	10.0000	1.0047	0.0975	3.2474	-0.6806	-0.7327	-0.5697	-0.0513	-0.4434	0.0463	15.7303
10	10	-25.3	10.0000	1.0000	0.0000	3.2474	-0.6806	-0.7327	-0.5670	0.0000	-0.4413	0.0000	15.7330

Zi(m)	u _g =U _g cosa	v _g =U _g sina	w _g	ū _g =axcosa	v̄ _g =axsina	w̄ _g	U _L	V _L	W _L	ū _L	v̄ _L	w̄ _L
0	14.3733	0.0000	1.5426	-1.4994	0.0000	1.5426	1.5426	0.0000	-14.3733	1.5426	0.0000	1.4994
-3	14.7415	0.0000	1.2161	-1.2129	0.0000	1.2161	1.2161	0.0000	-14.7415	1.2161	0.0000	1.2129
-6	15.0308	0.0000	0.9513	-0.9877	0.0000	0.9513	0.9513	0.0000	-15.0308	0.9513	0.0000	0.9877
-9	15.2558	0.0000	0.7345	-0.8126	0.0000	0.7345	0.7345	0.0000	-15.2558	0.7345	0.0000	0.8126
-12	15.4280	0.0000	0.5550	-0.6787	0.0000	0.5550	0.5550	0.0000	-15.4280	0.5550	0.0000	0.6787
-15	15.5559	0.0000	0.4036	-0.5791	0.0000	0.4036	0.4036	0.0000	-15.5559	0.4036	0.0000	0.5791
-18	15.6462	0.0000	0.2727	-0.5088	0.0000	0.2727	0.2727	0.0000	-15.6462	0.2727	0.0000	0.5088
-21	15.7034	0.0000	0.1556	-0.4643	0.0000	0.1556	0.1556	0.0000	-15.7034	0.1556	0.0000	0.4643
-24	15.7303	0.0000	0.0463	-0.4434	0.0000	0.0463	0.0463	0.0000	-15.7303	0.0463	0.0000	0.4434
-25.3	15.7330	0.0000	0.0000	-0.4413	0.0000	0.0000	0.0000	0.0000	-15.7330	0.0000	0.0000	0.4413

angle between the local and global axes			Transformation matrix			Transpose Matrix		
90	90	0	0	0	1	0	0	-1
90	0	90	0	1	0	0	1	0
180	90	90	-1	0	0	1	0	0

	wn=(V _L ² +w _L ²) ^{1/2}	%CDpDW	%CMpnD ¹	F _{dy}	F _{dz}	F _{ly}	F _{lz}	F _{x'}	F _{y'}	F _{z'}	F _x	F _y	F _z
0	14.37	15469.28	3864.16	0.00	-222345	0.00	5794.00	0.00	0.00	-216550.8	216551	0.00	0.00
-3	14.74	15865.58	3864.16	0.00	-233883	0.00	4686.68	0.00	0.00	-229196.2	229196	0.00	0.00
-6	15.03	16176.92	3864.16	0.00	-243152	0.00	3816.72	0.00	0.00	-239335.7	239336	0.00	0.00
-9	15.26	16419.09	3864.16	0.00	-250487	0.00	3140.07	0.00	0.00	-247346.7	247347	0.00	0.00
-12	15.43	16604.34	3864.16	0.00	-256171	0.00	2622.45	0.00	0.00	-253548.5	253549	0.00	0.00
-15	15.56	16742.05	3864.16	0.00	-260438	0.00	2237.64	0.00	0.00	-258200.3	258200	0.00	0.00
-18	15.65	16839.21	3864.16	0.00	-263469	0.00	1966.17	0.00	0.00	-261503.3	261503	0.00	0.00
-21	15.70	16900.73	3864.16	0.00	-265398	0.00	1794.27	0.00	0.00	-263603.8	263604	0.00	0.00
-24	15.73	16929.73	3864.16	0.00	-266310	0.00	1713.25	0.00	0.00	-264596.3	264596	0.00	0.00
-25.3	15.73	16932.62	3864.16	0.00	-266401	0.00	1705.16	0.00	0.00	-264695.4	264695	0.00	0.00
SUMMATION OF FORCES											2498577	0.00	0.00

Table 12: Excel program to generate the environmental forces acting on pillar 4

VERTICAL MEMEBER4													
Xi(m)	Yi(m)	Zi(m)	xc=xcosa	Coshk(z+d)	Sinhk(z+d)	Sinhkd	Cos(ut-kxc)	Sin(ut-kxc)	U	W	a _x	a _z	U _c =U+C
-10	10	0	-10.0000	3.3979	3.2474	3.2474	0.6806	-0.7327	-1.9267	1.7105	1.4994	1.5426	14.3733
-10	10	-3	-10.0000	2.7485	2.5602	3.2474	0.6806	-0.7327	-1.5585	1.3485	1.2129	1.2161	14.7415
-10	10	-6	-10.0000	2.2383	2.0025	3.2474	0.6806	-0.7327	-1.2692	1.0548	0.9877	0.9513	15.0308
-10	10	-9	-10.0000	1.8415	1.5463	3.2474	0.6806	-0.7327	-1.0442	0.8145	0.8126	0.7345	15.2558
-10	10	-12	-10.0000	1.5379	1.1684	3.2474	0.6806	-0.7327	-0.8720	0.6155	0.6787	0.5550	15.4280
-10	10	-15	-10.0000	1.3123	0.8497	3.2474	0.6806	-0.7327	-0.7441	0.4476	0.5791	0.4036	15.5559
-10	10	-18	-10.0000	1.1531	0.5741	3.2474	0.6806	-0.7327	-0.6538	0.3024	0.5088	0.2727	15.6462
-10	10	-21	-10.0000	1.0523	0.3275	3.2474	0.6806	-0.7327	-0.5966	0.1725	0.4643	0.1556	15.7034
-10	10	-24	-10.0000	1.0047	0.0975	3.2474	0.6806	-0.7327	-0.5697	0.0513	0.4434	0.0463	15.7303
-10	10	-25.3	-10.0000	1.0000	0.0000	3.2474	0.6806	-0.7327	-0.5670	0.0000	0.4413	0.0000	15.7330
Zi(m)	u _g =U _c cosa	vg=ucsinα	w _g	ū _g =axcosa	v _g =axsina	w _g	U _l	VL	W _l	ū _l	v _l	w _l	
0	14.3733	0.0000	1.5426	1.4994	0.0000	1.5426	1.5426	0.0000	-14.3733	1.5426	0.0000	-1.4994	
-3	14.7415	0.0000	1.2161	1.2129	0.0000	1.2161	1.2161	0.0000	-14.7415	1.2161	0.0000	-1.2129	
-6	15.0308	0.0000	0.9513	0.9877	0.0000	0.9513	0.9513	0.0000	-15.0308	0.9513	0.0000	-0.9877	
-9	15.2558	0.0000	0.7345	0.8126	0.0000	0.7345	0.7345	0.0000	-15.2558	0.7345	0.0000	-0.8126	
-12	15.4280	0.0000	0.5550	0.6787	0.0000	0.5550	0.5550	0.0000	-15.4280	0.5550	0.0000	-0.6787	
-15	15.5559	0.0000	0.4036	0.5791	0.0000	0.4036	0.4036	0.0000	-15.5559	0.4036	0.0000	-0.5791	
-18	15.6462	0.0000	0.2727	0.5088	0.0000	0.2727	0.2727	0.0000	-15.6462	0.2727	0.0000	-0.5088	
-21	15.7034	0.0000	0.1556	0.4643	0.0000	0.1556	0.1556	0.0000	-15.7034	0.1556	0.0000	-0.4643	
-24	15.7303	0.0000	0.0463	0.4434	0.0000	0.0463	0.0463	0.0000	-15.7303	0.0463	0.0000	-0.4434	
-25.3	15.7330	0.0000	0.0000	0.4413	0.0000	0.0000	0.0000	0.0000	-15.7330	0.0000	0.0000	-0.4413	
angle between the local and global axes			Transformation matrix						Transpose Matrix				
	90	90	0		0	0	1		0	0	-1		
	90	0	90		0	1	0		0	1	0		
	180	90	90		-1	0	0		1	0	0		
	wn=(VL ² +wl ²) ^{1/2}	%CDpDW	%CMprD ¹	Fdy	Fdz	Fiy	Fiz	Fx'	Fy'	Fz'	Fx	Fy	Fz
0	14.37	15469.28	3864.16	0.00	-222344.9	0.00	-5794.00	0.00	0.00	-228138.9	228139	0.00	0.00
-3	14.74	15865.58	3864.16	0.00	-233882.9	0.00	-4686.68	0.00	0.00	-238569.6	238570	0.00	0.00
-6	15.03	16176.92	3864.16	0.00	-243152.4	0.00	-3816.72	0.00	0.00	-246969.2	246969	0.00	0.00
-9	15.26	16419.09	3864.16	0.00	-250486.8	0.00	-3140.07	0.00	0.00	-253626.9	253627	0.00	0.00
-12	15.43	16604.34	3864.16	0.00	-256171.0	0.00	-2622.45	0.00	0.00	-258793.4	258793	0.00	0.00
-15	15.56	16742.05	3864.16	0.00	-260438.0	0.00	-2237.64	0.00	0.00	-262675.6	262676	0.00	0.00
-18	15.65	16839.21	3864.16	0.00	-263469.5	0.00	-1966.17	0.00	0.00	-265435.7	265436	0.00	0.00
-21	15.70	16900.73	3864.16	0.00	-265398.1	0.00	-1794.27	0.00	0.00	-267192.4	267192	0.00	0.00
-24	15.73	16929.73	3864.16	0.00	-266309.6	0.00	-1713.25	0.00	0.00	-268022.8	268023	0.00	0.00
-25.3	15.73	16932.62	3864.16	0.00	-266400.6	0.00	-1705.16	0.00	0.00	-268105.7	268106	0.00	0.00
SUMMATION OF FORCES											2557530	0	0

3.2 Shear Force

All forces acting on each member of the structure were summed to obtain the Shear force about the baseline of the structure

Table 13: Shear Force acting on the baseline of every pile

Members	FX (N)	FY (N)	FZ (N)
Vertical member1	2557530	0.00	0.00
Vertical member2	2498577	0.00	0.00
Vertical member3	2498577	0.00	0.00
Vertical member4	2557530	0.00	0.00
Total force	10112214	0.00	0

3.3 Software Simulation of the Structural Response to the Wave and Tidal Forces of the Columns

FEA is an analytical method based on approximate solutions to solve any complex engineering problem by subdividing the problems into smaller, more manageable elements. This analytical method involves three stages which are as follows:

Pre-processing stage:

This involves the construction of the element mesh, the definition of material properties, the boundary conditions.

Solution stage:

This involves allowing the ansys software to solve the computed model.

Post-processing stage:

This involves the visualisation and the analysing of the results obtained which is then used to understand the structural mechanism.

From Appendix A the element type used in modelling the columns is BEAM4 (3-D Elastic Beam) which has a uniaxial element with tension, compression, torsion, and bending capabilities. The element has six degrees of freedom at each node: translations in the nodal x, y, and z directions and rotations about the nodal x, y, and z axes. Stress stiffening and large deflection capabilities are included (ANSYSInc, 2007) The modelling strategy employed is the bottom up ap-

proach. This is to create key points that will establish the nodes of the different columns of the tank. These nodes are spaced 3m apart from each other and they form elements. The hydrodynamic forces act on these elements.

Table 14: tables specifying the modelling nodes for each column

Node	x	y	z
1	0	0	0
5	0	0	-3
9	0	0	-6
13	0	0	-9
17	0	0	-12
21	0	0	-15
25	0	0	-18
29	0	0	-21
33	0	0	-24
37	0	0	-25.3

Node	x	y	z
2	20	0	0
6	20	0	-3
10	20	0	-6
14	20	0	-9
18	20	0	-12
22	20	0	-15
26	20	0	-18
30	20	0	-21
34	20	0	-24
38	20	0	-25.3

Node	x	y	z
3	20	20	0
7	20	20	-3
11	20	20	-6
15	20	20	-9
19	20	20	-12
23	20	20	-15
27	20	20	-18
31	20	20	-21
35	20	20	-24
39	20	20	-25.3

Node	x	y	z
4	0	20	0
8	0	20	-3
12	0	20	-6
16	0	20	-9
20	0	20	-12
24	0	20	-15
28	0	20	-18
32	0	20	-21
36	0	20	-24
40	0	20	-25.3

3.4 Boundary Conditions

Boundary Restraints: The bases of all the columns were restrained from moving in all the directions.

Applied Loads

Submerged parts of the columns which is twenty five point three meters are divided into 10 numbers of divisions for each vertical column. Loads were generated and applied based on these divisions at an interval of 3m except for the last division which is 1.3m interval. All loads were applied on the elements at different nodes as incident wave and current forces are added together vectorially. An axial load due the weight of the tank and the weight of the life load (petroleum product) was applied at the top of the columns. The value of the axial force on each column is 9107114N (see Appendix B). The forces act on the elements of the columns, and large deformations were not considered because it is a linear analysis.

Solution

The pre-processing and post-processing phases of the finite element method are interactive through the solution phase. The governing equations are assembled into matrix form and are solved numerically. The analysis method depends on the element type of the model, material properties and boundary conditions.

Menu Paths

Main Menu>Solution>Solve>Current LS

Post Processing

When once the solution of the model has been done then, a post processing of the model takes place. This is the reading and plotting of the results obtained from Ansys and also comparing the nodal and element von misses stresses, including their displacements. A graph of the von misses stress values are plotted against the distances of their nodes apart.

3.5 Presentation of result

Failure criterion used: The failure prediction of the column model will be by the assessment of the von misses stress. The von misses stress is compared to the column yield stress and the ultimate strength given by the manufacturers of the steel column. The von misses stress failure criterion was chosen because it puts all the principal stresses into account to give an equivalent stress for more accurate prediction.

The principal stresses are

σ_1 = axial stress

σ_2 = hoop stress

σ_3 = radial stress

Von misses stress, $\sigma = (1/\sqrt{2}) \sqrt{[(\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_3 - \sigma_1)^2]}$

Nodal Solution

ANSYS calculates the nodal solution for each node. Therefore, the arrangement of the nodes is important to get better accuracy. The nodal Von misses stresses are compared to the element von misses stress (As shown in Appendix C). Minimum nodal von misses stress is 136568 Mpa
 Maximum nodal von misses stress is 0.567E+08Mpa

The Element Solution

Every element has its own stress region, because ANSYS calculates the element solution which is an average stress of the element. The element von misses stresses are the same as the nodal stresses (See Appendix D) Minimum element von misses stress is 136568 Pa
 Maximum element von misses stress is 0.567E+08 Pa

3.6 Interpretation of the Deformed Shape of the Pipe Line

The columns were displaced 0.082605m at the top but the bottom side remained stable to the sea bed. This is because the bases of the columns are firmly fixed to the sea bed and the top sides of the columns are exposed to the highest hydrodynamic forces. As shown in Appendix E). Summary of the results obtained from FEA

The following results are obtained from the FE Analysis from the response of the structure due to hydrodynamic loading and axial loading;

Table 15: Summary of Obtained results

Maximum Von misses stress	0.567E+08 Pa
Maximum Displacement	0.082605m
Maximum Tensile stress	0.29013E+07 Pa
Maximum Compressive stress	-0.20608E+03 Pa
Maximum bending stress	0.843E+08 Pa

Validation of Result

Design Code Check

Design Specification

The following design code was used to check against the integrity of the storage tank columns.

- API RP 2A 21st Edition, 1993-Recommended Practice for Planning Design and Constructing Fixed Off-shore Platform-Working Stress Design.

The columns structural response predicted using FEM is strength checked against the above mentioned design codes using the following;

Axial Tension

- $F_t = 0.6f_v = 0.6 \times 345 = 207N/mm^2$

Where $f_v = \text{Min yield stress in } N/mm^2$

- *Allowable Axial Compression*
 For $D/t \leq 60$

API sec 3.2.2 a

i.e. $2/1 \leq 60$

$$\frac{KI}{r} = \frac{1.0 \times 25.3}{0.499} = 50.7$$

Where $k = \text{constant} = 1$

$L = \text{length of column}$

$R = \text{Radius of gyration}$

and $C_c = \left[\frac{2\pi^2 E}{f_y} \right]^{1/2} = \left[\frac{2 \times \pi^2 \times 210}{345} \right]^{1/2} = 3.466$

Since $\frac{KI}{r} > C_c$

Therefore the option below is used

$$F_a = \frac{14700}{\dots} = \frac{14700 \times 345}{\dots} = 420N/mm^2$$

Allowable Bending Stress

For $\frac{KI}{r} < 1.5$
 $\frac{300}{1c}$ API sec 3.2.3-

Use

$$F_b = \left[0.72 - 0.58 \frac{f_y}{\dots} \right] f_y = \left[0.72 - 0.58 \frac{345}{\dots} \right] 345 \times 10^6 = 247.26N/mm^2$$

- *Allowable Shear Stress*

$$F_v = 0.4f_v$$

API sec 3.3.4-a

$$= 0.4 \times 345 = 138N/mm^2$$

- *Allowable Von Mises*

$$0.8F_v = 0.8 \times 345 = 276N/mm^2$$

The results obtained from the design code shows that the allowable axial tensile, Compressive, bending and Von mises stress are 207N/mm², 209N/mm², 228.67N/mm² and 276N/mm² respectively [9].

Table 16 Result comparison

Prediction	Finite Element Method	Design Code- Allowable
Axial Tension	2.9 N/mm ²	207N/mm ²
Axial Compression	0.000206 N/mm ²	4207N/mm ²
Bending	84.3 N/mm ²	247.26N/mm ²
Von mises	56.7 N/mm ²	276N/mm ²

3.7 Overall Presentation of the Report

The highest stress concentration occur at the base of the columns. This is inline with bending moment and shear force theory of a cantilever. Therefore in the actual design of the columns the base section of the columns should be reinforced to withstand the stress and the be

Wind

Proper analysis of wind data can be used to determine the wind criteria for the design of the storage system. As with wave load, wind loads are dynamic in nature, but some structure will respond to them in nearly static fashion. For conventional fixed steel structures in relatively shallow water the contribution of wind to global loads is typically less than 10%. Sustained wind velocities will be used to compute global platform wind loads and gust velocities will be used for the design of individual structural elements.

Wind Properties.

There is variation of wind speed and direction in space and time. On length scales typical of even large offshore structures, statistical wind properties (e.g. mean and standard deviation of velocity) taken over durations of the order of an hour do not vary horizontally, but is said to change with elevation (profile factor). Within long durations there will be shorter durations with higher mean speeds (gust factor), this means that a wind speed value is meaningful if qualified by its elevation and duration.

Wind Velocity and Force Relationship

From the API specification, the wind force on an object should be calculated by using the appropriate method such as:

$$F = (w/2g)(V^2)C_s A$$

Where:

F = wind force

W=weight density of air

g = gravitational acceleration

V = wind speed

C_s = shape coefficient

A = area of object

The recommended shape coefficient C_s for a perpendicular wind to the storage tank is 0.5

Therefore Force = 10.4/(2x9.81)x16²x0.5x2x3.14x12.954x12.192

WIND FORCE= 67294.99N

4 Conclusions

The objective of this project is to accurately predict the response of cylindrical columns under hydrodynamic wave forces and current using the finite element method.

The type of analysis employed to achieve this objective is the linear analysis. This analysis means that due to the applied hydrodynamic forces on the columns, a resultant deformation of the column is seen which is directly proportional to all the inputs such as the applied loads, F , stiffness, K from material properties, geometry, and restraints. Thus, $X=F/K$, such that if the load is doubled, the deformation is doubled. If stiffness is doubled, the deformation is halved.

The columns were restrained at the base in all directions. It was assumed that the columns are firmly fixed to the sea bed and the foundations of the sea bed are strong and immovable. This means the application of hydrodynamic forces due to the waves and currents on the columns will not cause the columns to move at the base in any direction.

We assume that the deflection of the material under load is small and linear.

The stiffness of the column material is determined by the material properties and the geometry of the column. The material properties required to simulate this kind of column analysis is divided into two parts.

Input properties are properties required to calculate a response by the material. The properties are Young's Modulus and Poisson ratio

Failure properties are properties needed to interpret the response. They are Yield strength and the ultimate strength
The material properties employed are the ones given above under the section column data and material properties.

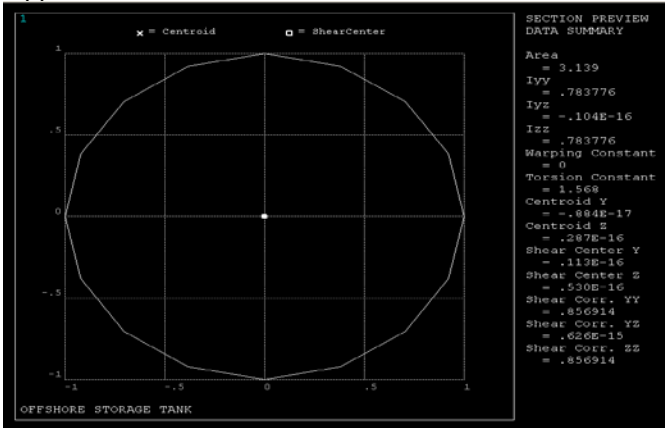
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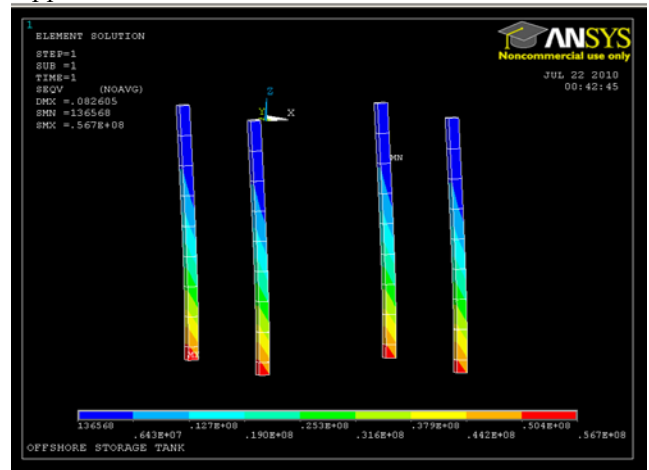
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COLUMN SHAPE AND SECTION PROPERTIES GENERATED FROM ANSYS

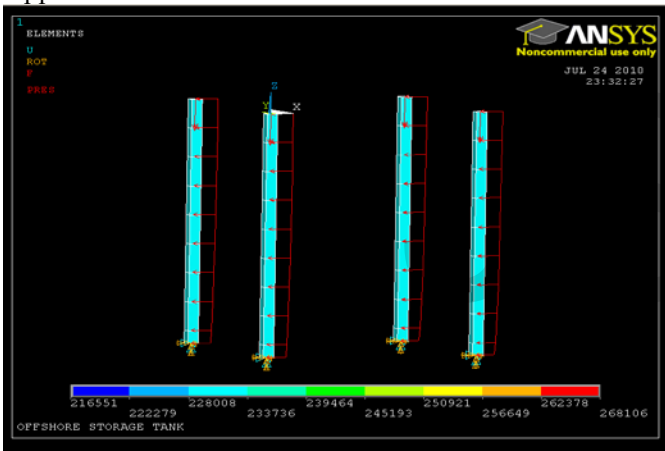
Appendix A



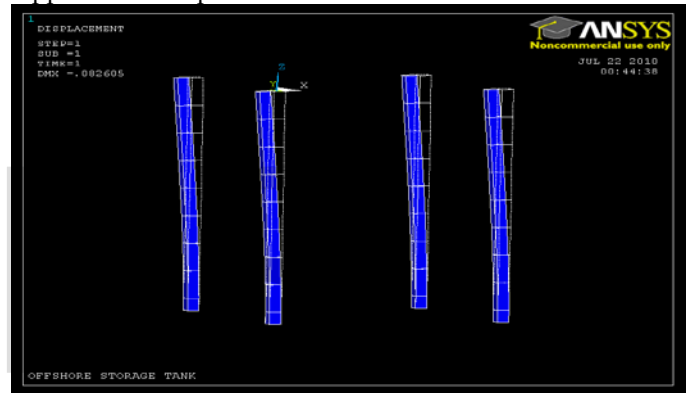
Appendix D: Element Solution



Appendix B



Appendix E: Displacement



Axial load, lateral hydrodynamic pressures and maximum constraints at the base of the columns

Appendix C: Nodal Solution

